

IV II & RDD II

PMP 8521: Program Evaluation for Public Service

November 18, 2019

**Fill out your reading report
on iCollege!**

PLAN FOR TODAY

Instruments

Treatment effects and compliance

Fuzzy RD

Synthetic data with R

INSTRUMENTS

WHAT IS AN INSTRUMENT?

Something that is correlated with the policy variable

Something that does not directly cause the outcome

Something that is not correlated with the omitted variables

Relevance

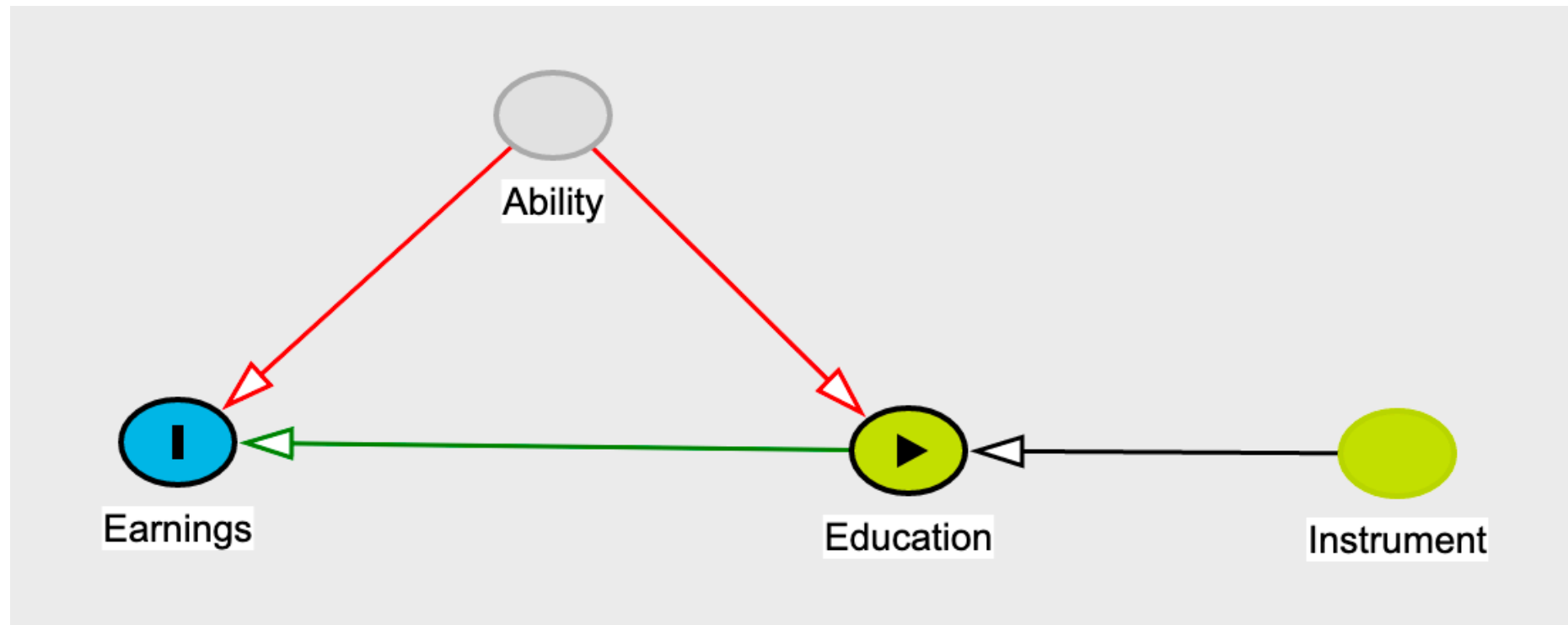
Testable with stats!

Exclusion

("only through")

Not testable!

Exogenous



TREATMENT EFFECTS & COMPLIANCE

POTENTIAL OUTCOMES

$$\delta = (Y|P = 1) - (Y|P = 0)$$

δ = Causal impact of program

P = Program

Y = Outcome

$$\delta = Y_1 - Y_0$$

Fundamental problem of causal inference

$$\delta_i = Y_i^1 - Y_i^0$$

Individual-level effects are
impossible to observe

AVERAGE TREATMENT EFFECT

Difference between expected value when program is on vs. expected value when program is off

$$ATE = E(Y_1 - Y_0) = E(Y_1) - E(Y_0)$$

Can be found for a whole population, on average

$$\delta = (\bar{Y} | P = 1) - (\bar{Y} | P = 0)$$

**Every individual has a
treatment/causal effect**

**ATE = average of all
unit-level causal effects**

**ATE = average effect
for the whole population**

VERSIONS OF CAUSAL EFFECTS

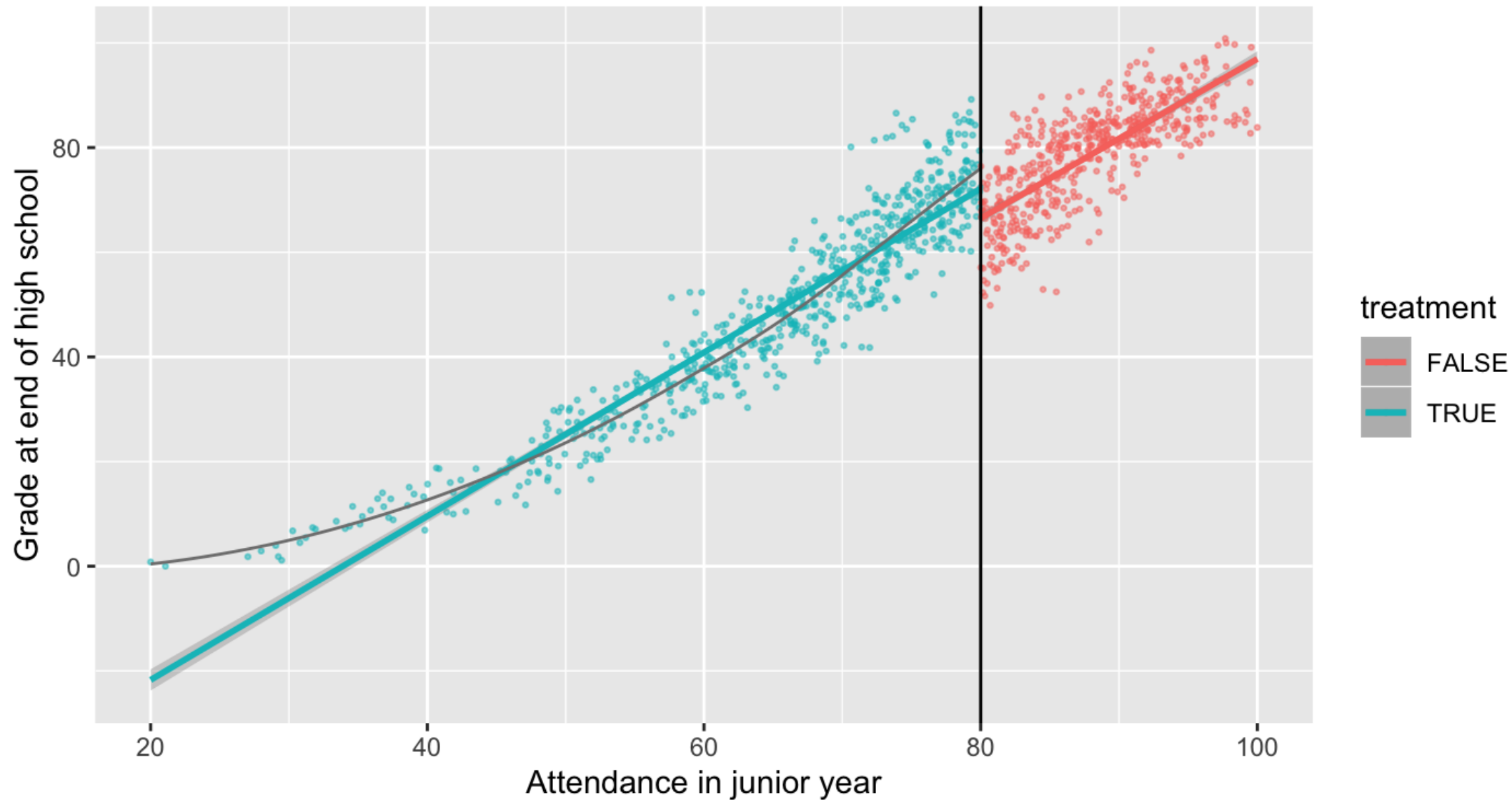
Average treatment on the treated

ATT / TOT

Conditional average treatment effect

CATE

LOCAL EFFECTS



LATE

**Local average treatment effect (LATE) =
weighted ATE**

Narrower effect; only includes some of the population

**Can't make population-level
claims with LATE**

(But that can be okay)

LATE

In RDD, LATE = people in the bandwidth

In RCTs, IVs, etc., LATE = compliers

COMPLIANCE

Compliers

Treatment follows assignment

Always takers

Gets treatment regardless of assignment

Never takers

Rejects treatment regardless of assignment

Defiers

Does opposite treatment from assignment

Choice if assigned to treatment



Choice if assigned to control

Y Y

Y Y

Y Y

Y Y

Always takers

N N

N N

N N

N N

Never takers

Y N

Y N

Y N

Y N

Compliers

IGNORING DEFIERERS

We can generally assume defiers don't exist

In drug trials this makes sense; can't get access to medicine without being in treatment

In development, it can make sense; in a bed net RCT, a defier assigned to treatment would have to tear down all existing bed nets out of spite

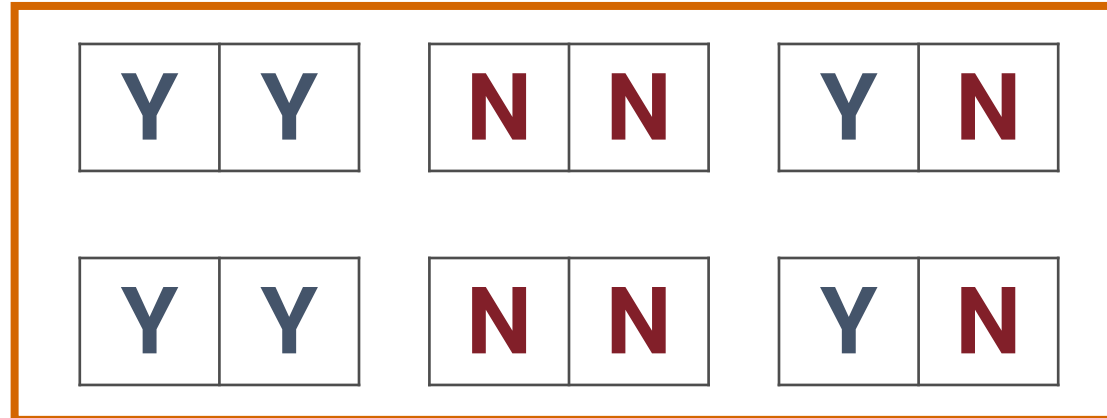
IGNORING DEFIERS

Monotonicity assumption

Assignment to treatment only
has an effect in one direction

Assignment to treatment can only increase—
not decrease—your actual chance of treatment

Population



Always takers

Never takers

Compliers

Assigned to treatment

Always
takers &
compliers



Never
takers



Assigned to control

Always
takers



Never
takers &
compliers



MORE EFFECTS

Intent to treat (ITT)

Effect of assignment (not actual treatment!)

Assigned to treatment

Always
takers &
compliers

Y

Y

Never
takers

N

N

Assigned to control

Always
takers

Y

Y

Never
takers &
compliers

N

N

MORE EFFECTS

Complier Average Causal Effect (CACE)

LATE for the compliers

Assigned to treatment

Always
takers &
compliers

Y

Y

Never
takers

N

N

Assigned to control

Always
takers

Y

Y

Never
takers &
compliers

N

N

Assigned to treatment

Always
takers &
compliers



Never
takers



Assigned to control

Always
takers



Never
takers &
compliers



$$\begin{aligned} \text{ITT} = & \pi_{\text{compliers}} \times (\text{T} - \text{C})_{\text{compliers}} + \\ & \pi_{\text{always takers}} \times (\text{T} - \text{C})_{\text{always takers}} + \\ & \pi_{\text{never takers}} \times (\text{T} - \text{C})_{\text{never takers}} \end{aligned}$$

$$\text{ITT} = \pi_{\text{C}} \text{CACE} + \pi_{\text{A}} \text{ATACE} + \pi_{\text{N}} \text{NTACE}$$

$$ITT = \pi_C CACE + \pi_A ATACE + \pi_N NTACE$$

$$ITT = \pi_C CACE + \pi_A 0 + \pi_N 0$$

**Exclusion restriction;
treatment received is same
regardless of assignment**

$$ITT = \pi_C CACE$$

$$CACE = \frac{ITT}{\pi_C}$$

$$\text{CACE} = \frac{\text{ITT}}{\pi_C}$$

$$\text{ITT} = (\bar{y}|\text{Treatment}) - (\bar{y}|\text{Control})$$

Assigned to treatment

$\pi_A + \pi_C$



π_N



Assigned to control



π_A



$\pi_N + \pi_C$

$\pi_A + \pi_C = \% \text{ in treatment and yes}$

$\pi_C = \% \text{ in treatment and yes} - \pi_A$

$$\text{CACE} = \frac{\text{ITT}}{\pi_C}$$

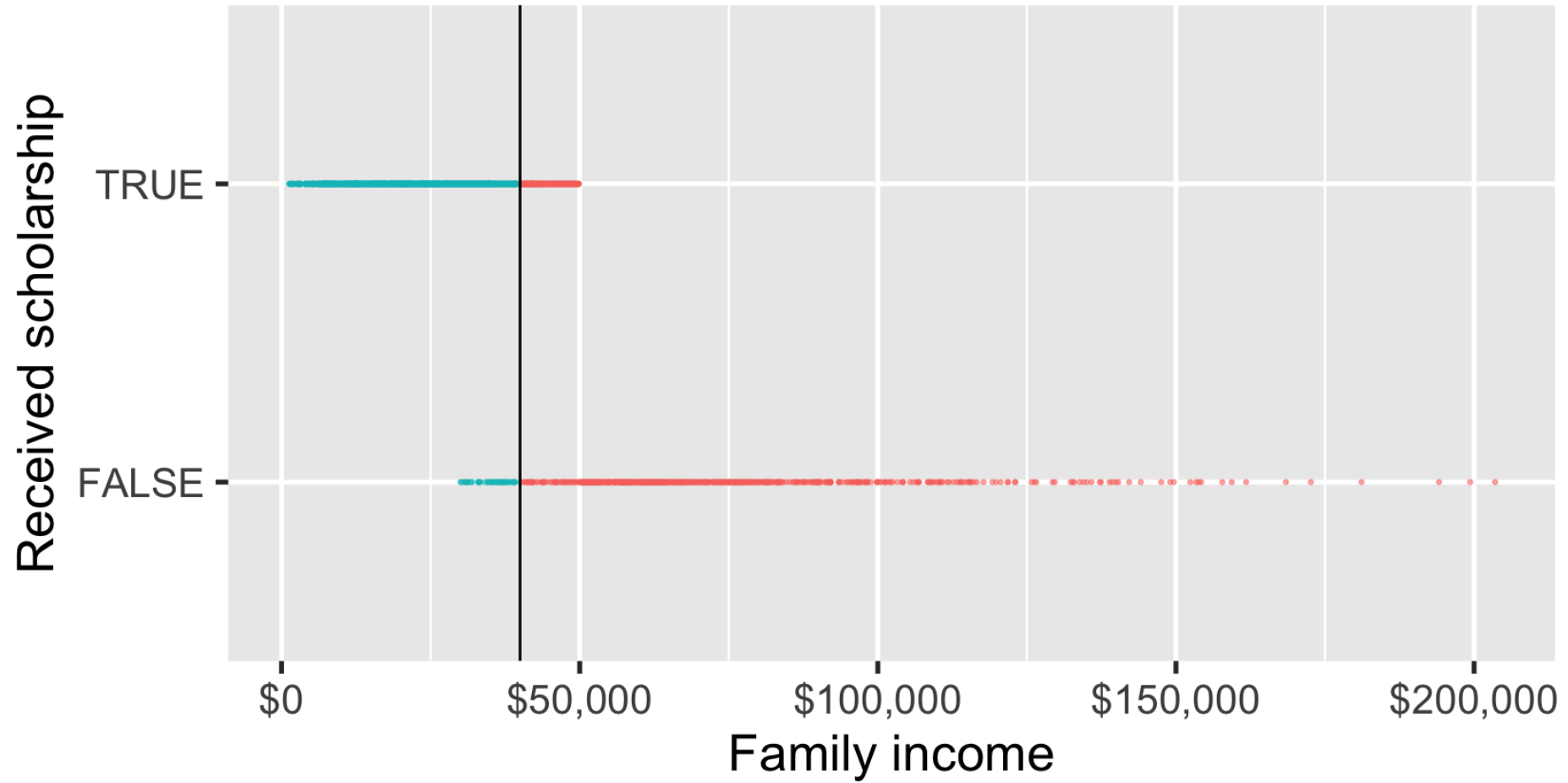
$$\text{ITT} = (\bar{y}|\text{Treatment}) - (\bar{y}|\text{Control})$$

π_C = % in treatment and yes—
 % in control and yes

Example in R

FUZZY RD

oh no



Income < \$40,000: ● FALSE ● TRUE

Use an instrument to deal with noncompliance

Often actual participation in
program works as instrument

SYNTHETIC DATA WITH R